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INVESTIGATION OF THERMAL NEUTRON FLUX
PERTURBATION IN A POLYETHYLENE MEDIUM
BY USE OF GOLD FOIL DETECTORS

EDWARD C. COPELAND
and
ROGER L. REASONOVER, JR.

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MEDIUM BY USE OF GOLD FOIL DETECTORS

* * * * *

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Submitted in partial fulfillment of
the requirements for the degree of

MASTER OF SCIENCE

IN

PHYSICS

United States Naval Postgraduate School
Monterey, California

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INVESTIGATION OF THERMAL NEUTRON
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ABSTRACT

The neutron flux perturbation in a homogeneous thermal reactor, polyethylene moderated, was investigated experimentally through use of activated gold foils of varying thicknesses. The experimental data are compared with the theoretical predictions of Bothe and Skyrme, and with the modifications introduced by Tittle and by Ritchie and Eldridge.

Experimental determination of the thermal neutron flux at the center of the core of the AGN-201 reactor indicates that Skyrme's theory and/or Skyrme's theory as modified by Ritchie and Eldridge give the best results over a range of foil thickness from two to ten mils. The greatest deviation of theoretical calculations from experimental data is less than 3%.

Determinations of other investigators for gold detectors in graphite agree to within 3% with the predictions of the Skyrme theory. In water-moderated reactors experimental determinations have been compared with the Skyrme theory as modified by Ritchie and Eldridge and found to agree to 5%.

The writers wish to express their appreciation to Professor William W. Hawes of the U.S. Naval Postgraduate School for his patient assistance and encouragement during this investigation.

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The foils were mounted for counting on a 0.054 inch thick plexiglass tray at a sample-to-crystal distance of three cms. The tray was of adequate thickness to reduce beta radiation to an insignificant amount. The sample tray was mounted in a plastic holder which, together with the NaI crystal and photomultiplier tube, was mounted inside a lead shield as described by Clements and Kelly (6). By this arrangement the backscatter was less than 4% of the total measured activity. Figure 8 (Appendix II).

The absolute disintegration rate was calculated from the measured activity by the relation:

$$R^0(x) = \frac{N_p}{f_e \cdot f_s \cdot f_{ic} \cdot R_{pt} \cdot (1 - \exp[-\lambda T]) \cdot \exp(-\lambda t)} \quad (II)$$

The total number of events per second under the photopeak, N_p , was computed following the method of Clements and Kelly (6). The values for crystal detection efficiency and peak-to-total ratio are 0.118 and 0.725, respectively, as determined by Heath (7,8). The value of the internal conversion factor is given by Raffle (9) as 0.96. Sola (10) gives the following equation for self-absorption in the foil:

$$f_s = \frac{1 - \exp(-\mu d)}{\mu d}$$

Cooke (11) calculated the spectral-hardening effect in the AGN-201 reactor which results in an effective thermal energy of 0.0296 ev vice the accepted 0.0253 ev. Employing the technique of Meadows (12) and Westcott (13), an average effective thermal cross-section for this value of thermal energy was calculated and found to be 88.3 barns. Clements and Kelly (6) found a Cadmium ratio for this reactor to be 5.36, which gives a ratio of thermal activations in the foil to total activations equal to 0.815. This ratio will not be constant over the entire range of foil thicknesses, but the error may be neglected as it is less than 1%

at its maximum value (13). The average flux in the foil may then be calculated in the conventional manner using the expression:

$$\phi_t = \frac{0.815 R^0(x) W}{N_o \sigma_a m} \quad (III)$$

For each foil thickness, three separate determinations were made; in each determination the foil was counted three times giving nine values of $R^0(x)$ for each increment of thickness between two and ten mils. Counting procedures insured statistical precision to within 1%. The experimental data obtained are given in Table III with the maximum deviation for each thickness.

Table III

d (mils)	N_p (counts/sec)	$R^0(x)$ (counts/sec)	ϕ_t (neut/cm ² sec)	ϕ_t (max deviation)
2	2.87×10^4	1.41×10^5	3.43×10^6	-0.15×10^6
4	2.36×10^4	2.61×10^5	3.19×10^6	$+0.11 \times 10^6$
6	2.27×10^4	3.62×10^5	2.94×10^6	$\pm 0.12 \times 10^6$
8	2.20×10^4	4.25×10^5	2.59×10^6	$+0.08 \times 10^6$
10	2.47×10^4	5.04×10^5	2.46×10^6	-0.27×10^6

The thermal neutron flux in the undisturbed medium, ϕ_o , is given by:

$$\phi_o = \frac{\phi_t}{F} \quad (IV)$$

where F is the appropriate theoretical correction factor as listed in Table I.

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4. RESULTS

The nine experimental determinations of ϕ_t for each foil thickness were averaged in accordance with standard statistical procedures. The mean values and their standard deviations are given in Table IV. Values of ϕ_o were calculated from the various theories using the factors listed in Table I; these are shown in the last four columns of Table IV. It is evident that a constant value for ϕ_o is not obtained in any case.

Table IV

d (mils)	$\phi_t \times 10^6$ (neut/cm ² sec)	Standard error for ϕ_t	ϕ_o ($\times 10^6$ neut/cm ² sec)			
			Bothe	Tittle	Skyrme	Ritchie
2	3.43	0.03	3.70	3.71	3.76	3.75
4	3.19	0.03	3.63	3.65	3.74	3.74
6	2.94	0.03	3.53	3.55	3.68	3.66
8	2.59	0.02	3.25	3.28	3.42	3.41
10	2.46	0.07	3.22	3.26	3.43	3.41

Figure 5 shows the experimental data fitted to a straight line by the "least squares" procedure. The straight-line fit is consistent with the experimental results of other investigators. Zobel (14) has made a rather precise and exhaustive investigation into water-moderated systems through gold foil exposure. His results show that, for the range from one to ten mils, the plot of thermal flux versus foil thickness is indeed a straight line within the limits of experimental accuracy. Bach (15) has determined that the binding effects on the neutron spectra will be quite similar for polyethylene and water molecules, differing by a maximum of $\sim 15\%$. Therefore, the perturbation curves should be similar in appearance, which justifies the straight line interpretation of the experimental curve in Figure 5.

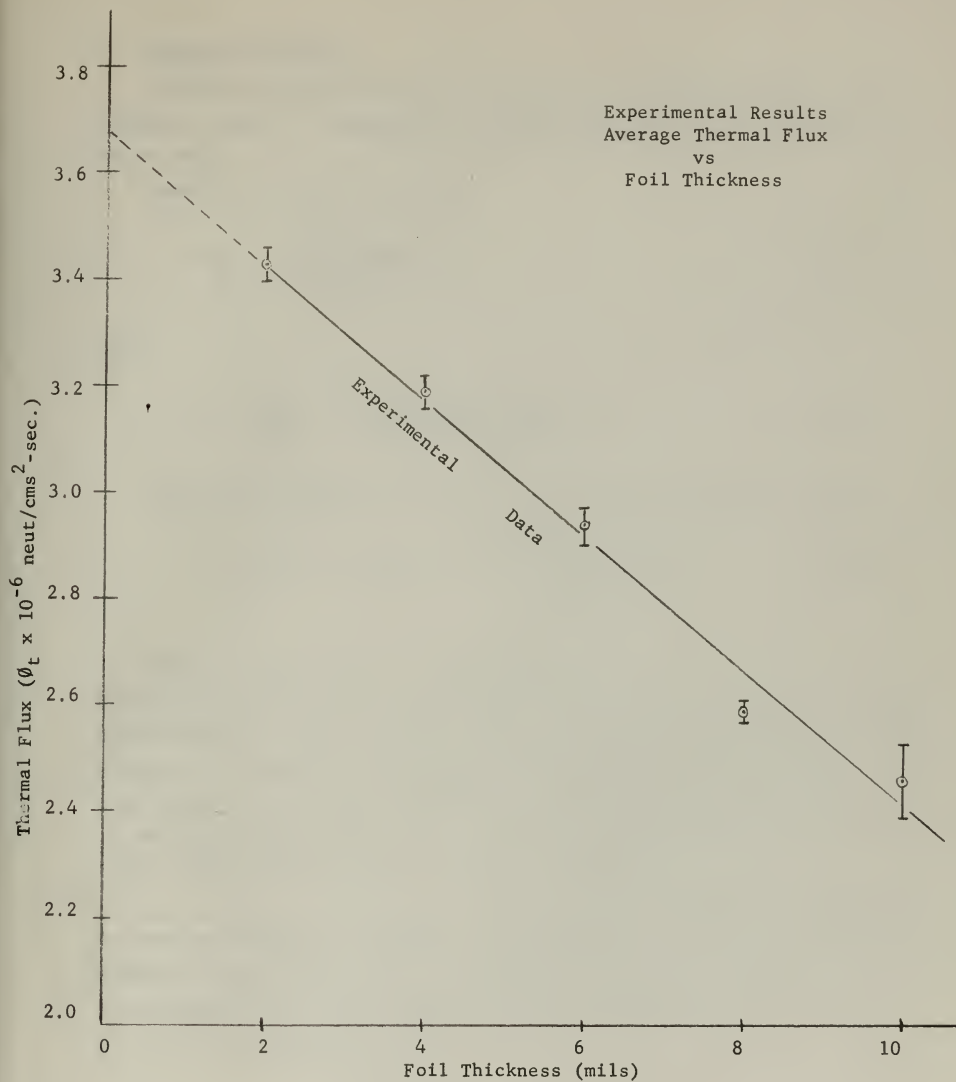


Figure 5

5. ANALYSIS OF RESULTS

Ritchie and Eldridge (5) proposed a method of analysis which, in essence, consist of comparing the various factors for flux depression effect only.

Equation III may be written:

$$\phi_t = \frac{0.815 R^0(x)}{\pi r^2 x} \quad (V)$$

and:

$$F = \frac{\phi_t}{\phi_o} = \frac{\left[\frac{1}{2} - E_3(x) \right] \frac{1}{x}}{1 + \left[\frac{1}{2} - E_3(x) \right] g} \quad (VI)$$

Substituting Equation (V) for ϕ_t in Equation (VI) and rearranging:

$$1 + \left[\frac{1}{2} - E_3(x) \right] g = \frac{c \left[\frac{1}{2} - E_3(x) \right]}{R^0(x)} \quad (VII)$$

where c is a constant of proportionality.

From Equation (VII), it is easily shown that the zero thickness intercept, multiplied by c , must equal one. Before the data can be plotted, for comparison, it is necessary that they be normalized consistent with the intercept value. To do this, c was evaluated for the two thinnest foils by each of the theoretical treatments. The values so obtained varied from 5.64×10^6 to 5.82×10^6 with a mean of $5.76 \pm .08 \times 10^6$. *

* From the equations involved, c is also seen to be equal to $\phi_o \pi r^2 / 0.815$; however, this relation cannot be employed for a reliable evaluation of ϕ_o . For comparison with final results, this relationship yields a value of $\phi_o = 3.70 \times 10^6$ neut/cm² sec.

Figure 6

Comparison of Flux Depression
with Experimental Data.

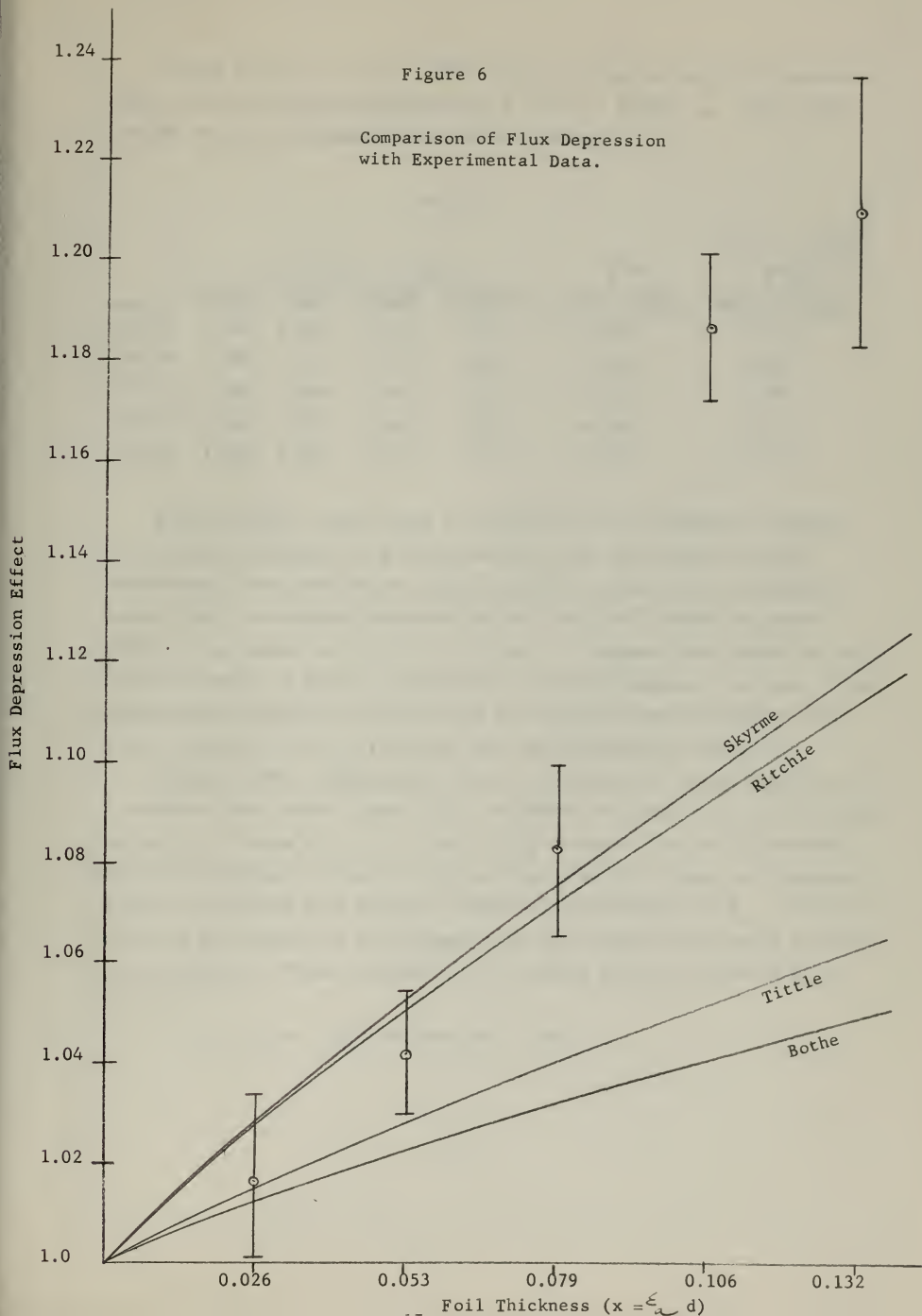


Figure 6 is a plot of $c [1/2 - E_3(x)] / R^0(x)$ versus foil thickness along with the theoretical values of $1 + [1/2 - E_3(x)]$ g. The values for the various thicknesses are given in Table V.

Table V

x	$1 + [1/2 - E_3(x)]$ g				$R^0(x)$	$c [1/2 - E_3(x)] / R^0(x)$
	Bothe	Tittle	Skyrme	Ritchie	($\times 10^5$ c/sec)	(Expr'l Data)
0.0264	1.012	1.015	1.028	1.027	1.406	1.016
0.0528	1.022	1.028	1.053	1.051	2.612	1.042
0.0792	1.032	1.040	1.076	1.073	3.618	1.083
0.1056	1.041	1.052	1.098	1.093	4.249	1.187
0.1320	1.049	1.063	1.119	1.112	5.036	1.210

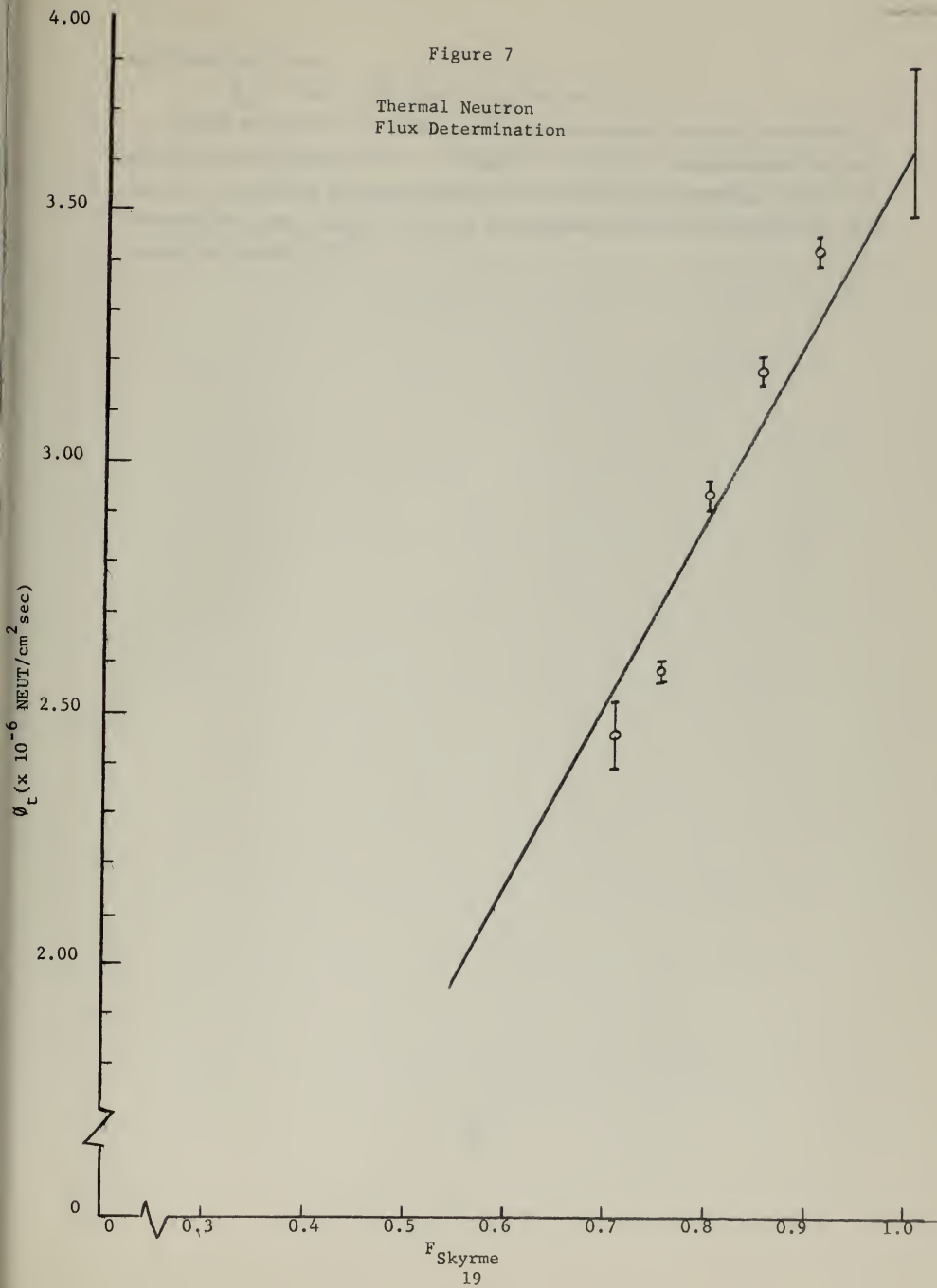
Figure 6 shows that there is actually little difference between the results of Skyrme and Ritchie and that our results more closely approximate these predictions, particularly at small foil thicknesses. Indeed, only the single determination at 2 mils is, within estimated error, in agreement with Tittle or Bothe. It appears that either of the first two might be used to extrapolate to zero thickness. In view of the approximate character of Ritchie and Eldridge's second correction, the g_v/g_s^∞ multiplier to g_s , the data have been extrapolated using g_s .

Equation (IV), rearranged, gives: $\phi_t = \phi_o F$ which is the equation of a straight line, whose slope is ϕ_o , and whose end-points are at the origin and at $F_s = 1$ where $\phi_t = \phi_o$. A plot of ϕ_t versus F_s for the five experimentally determined values of thermal flux plus the origin as a necessary sixth point should give the best possible determination of ϕ_o . In Figure 7 the data are plotted in this manner with the straight line being fitted by the procedure of "least squares". This yields from the value of ϕ_t at $F_s = 1$:

$$\phi_o = 3.64 \times 10^6 \text{ neutrons/cm}^2 - \text{sec.}$$

Figure 7

Thermal Neutron
Flux Determination



and from the slope:

$$\phi_0 = 3.68 \times 10^6 \text{ neutrons/cm}^2 - \text{sec.}$$

Their mean value is 3.66×10^6 which is also the value to which ϕ_t extrapolates linearly to $x = 0$ (Figure 5). From a consideration of all factors (including counting statistics, geometry of counting, errors in irradiation power level, etc.) it is estimated that the statistical precision is within $\pm 5\%$.

6. CONCLUSIONS

- (1) $\phi_0 = 3.66 \pm 0.18 \times 10^6$ neutrons/cm² - sec.
- (2) From this investigation, it is not possible to give preference to either Skyrme's or Ritchie's method of flux perturbation calculation in a polyethylene diffusion medium; however, either is more nearly correct than Bothe's and Tittle's calculations.
- (3) A very good value of ϕ_0 may be obtained by determining a number of values of ϕ_t between two and ten mils, and using a straight line extrapolation to zero thickness.

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APPENDIX I

EXPERIMENTAL DATA

All data given below are expressed in terms of Channel Number on the 50 Channel Step-Scanning Spectrometer and in counts per minute for the gamma activity. The counting rate has been corrected for background as given on page 29 . This background determination is the average of twenty separate counting runs made over a period of two weeks.

SAMPLE *1 - Two mils
February 7, 1961
Mass = 0.1273 gms.

<u>Channel</u>	<u>Run No. 1</u>	<u>Run No. 2</u>	<u>Run No. 3</u>
22	249	228	193
23	301	264	270
24	959	825	895
25	4193	3456	3541
26	9137	8111	7903
27	9656	9141	9355
28	4727	5087	4890
29	1179	1346	1258
30	167	187	203
31	75	75	93

SAMPLE *2 - Two mils
February 8, 1961
Mass = 0.1260 gms.

<u>Channel</u>	<u>Run No. 1</u>	<u>Run No. 2</u>	<u>Run No. 3</u>
22	178	191	181
23	281	234	226
24	967	748	614
25	3903	3250	2657
26	8691	7710	6963
27	8914	9516	9428
28	4223	5600	6114
29	922	1557	1779
30	142	254	285
31	47	69	61

SAMPLE *3 - Two mils
February 9, 1961
Mass = 0.1270 gms.

<u>Channel</u>	<u>Run No. 1</u>	<u>Run No. 2</u>	<u>Run No. 3</u>
22	323	203	203
23	446	309	279
24	1918	1217	1209
25	6625	4705	4404
26	10034	9221	9003
27	7651	8855	8988
28	2775	4189	4097
29	486	867	967
30	78	139	148

SAMPLE *4 - Two mils
February 10, 1961
Mass = 0.1160 gms.

<u>Channel</u>	<u>Run No. 1</u>	<u>Run No. 2</u>	<u>Run No. 3</u>
22	187	237	217
23	235	231	224
24	789	662	679
25	3310	2948	2808
26	7686	7083	7034
27	8964	8939	8911
28	4883	5281	5341
29	1239	1437	1547
30	163	209	250

SAMPLE *5 - Four Mils
February 13, 1961
Mass = 0.2543 gms.

<u>Channel</u>	<u>Run No. 1</u>	<u>Run No. 2</u>	<u>Run No. 3</u>
22	404	399	374
23	577	496	460
24	1967	1666	1674
25	7655	6851	6718
26	16250	15390	15048
27	16782	17113	17444
28	8364	8870	9340
29	2094	2287	2418
30	351	331	398
31	119	127	116

SAMPLE *6 - Four Mils
 February 14, 1961
 Mass = 0.2410 gms.

<u>Channel</u>	<u>Run No. 1</u>	<u>Run No. 2</u>	<u>Run No. 3</u>
22	188	178	155
23	227	184	190
24	560	511	499
25	2386	2360	2314
26	6092	6035	5933
27	8109	8051	8148
28	5004	4994	5317
29	1425	1409	1494
30	240	227	246
31	58	52	58

SAMPLE *7 - Four Mils
 February 14, 1961
 Mass = 0.2583 gms.

22	187	187	176
23	210	202	205
24	556	546	528
25	2293	2373	2247
26	6271	6341	6316
27	8585	8601	8510
28	5521	5631	5575
29	1697	1649	1635
30	264	277	279
31	46	71	58

SAMPLE *8 - Six Mils
 February 15, 1961
 Mass = 0.3931 gms.

23	236	248	202
24	919	738	711
25	3255	3121	2917
26	6976	6773	6610
27	7045	7233	7537
28	3414	3594	3667
29	751	951	865
30	114	158	143
31	44	51	39

SAMPLE *9 - Six Mils

February 15, 1961

Mass = 0.3814 gms.

<u>Channel</u>	<u>Run No. 1</u>	<u>Run No. 2</u>	<u>Run No. 3</u>
23	225	220	230
24	732	728	766
25	2940	3154	2852
26	6753	6738	6604
27	7383	7323	7328
28	3714	3646	3916
29	926	857	1014
30	124	125	143

SAMPLE *10 - Six Mils

February 15, 1961

Mass = 0.3974 gms.

23	199	221	234
24	748	650	737
25	2948	2694	2854
26	6881	6724	6688
27	7826	7753	7821
28	4311	4270	4242
29	1113	1022	1160
30	160	166	167

SAMPLE *11 - Eight Mils

February 16, 1961

Mass = 0.5044 gms.

22	191	206	155
23	325	260	249
24	1182	992	949
25	4864	3714	3350
26	7340	7184	6892
27	6468	6762	6594
28	2594	2823	2929
29	492	590	691
30	94	78	110

